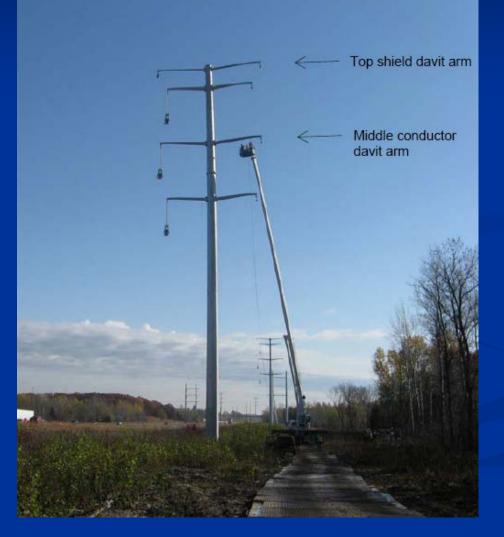
DAVIT ARM VIBRATION STUDY Double Circuit 345 kV Line





September 11-13, 2013



Background for the Study

- A mid-west utility is building a new 345 kV D.C. line and is installing complete structures (both sets of arms) but only one circuit will be strung. The second circuit will be installed when electrical load demands such.
- The pole suppliers recommended either suspending 150 lbs or 10% of the arm weight at the end of the unloaded arms "as a rule of thumb".
- The utility sought a better understanding of the proposed tuned-mass damping.





Our Prior Experience: November, 2005 – Wisconsin

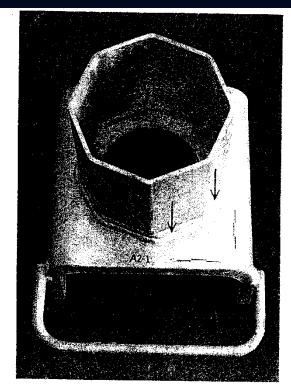


Both circuits were scheduled to be strung in but the unloaded arms stood for 39 days and failed before the static wires could be installed. Our experience with this topic started in 2005 when static arms for a double circuit 345 kV line started coming down shortly after installation.





As part of the design team, we were involved in the post-failure investigation. We worked with the Owner, an independent laboratory, and the pole vendor, but not everyone shared the same theory as to the root cause of failure:



Photograph No. 1

The photograph displays one of the three failed weldments, designated as the A2-1 Shield Wire Arm, Part No. 05-10112, joining the indicated component sections of their octagonal shafts to their arm brackets. The three units developed cracks but did not fracture through the entire weld surrounding the shaft. The red arrows bracket the location where the UT inspection indicated a crack was present.

"Also the pictures of the arms that failed in the field do not support failure due to Vortex shedding. Cracking appears to have started along the sides. Vortex shedding causes movement perpendicular to the direction of the wind, therefore cracking should have propagated from the top or bottom of the arm (see attached photo)." – Vendor Engineer



Davit arms represent a bluff structure. A bluff structure is one in which the flow separates from large sections of the structure's surface. 345 kV davit arms are very long slender structures that are prone to vortex shedding

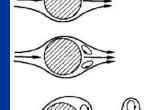
Re = Reynolds Number, a measure of the ratio of inertial to viscous forces. Re=Uf*D/n

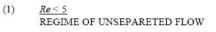
Where

Uf = velocity of the fluid w.r.t. the object (wind speed)

D = mean diameter n= kinematic viscosity

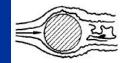
For tubular steel arms and shafts, Re $\sim 10^5$

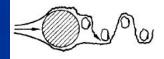




-) <u>5 TO 15 < Re < 40</u> A FIXED PAIR OF F_PPL VORTICES IN WAKE
-) <u>40 < Re < 90 AND 90 < Re < 150</u> TWO REGIMES IN WHICH VORTEX STREET IS LAMINAR

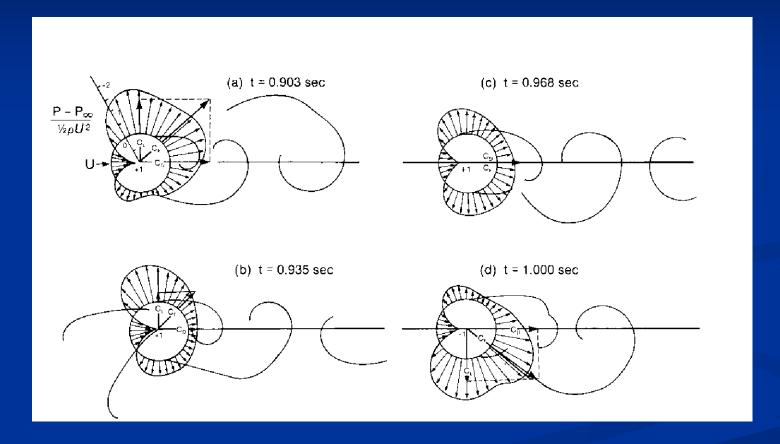






-) <u>150 < Re < 300</u> TRANSITION RANGE TO TURBULENCE IN VORTEX
- (5) <u>3x10³ < Re < 3.5x10⁶</u> LAMINAR BOUNDARY LAYER HAS UNDERGONE TURBULENT TRANSITION AND WAKE IS NARROWER AND DISORGANIZED
- (6) <u>5.6x10⁶ < *Re*</u> RE-ESTABLISHMENT OF TURBULENT VORTEX STREET

This causes an oscillating pressure differential



That does not act solely in the vertical plane



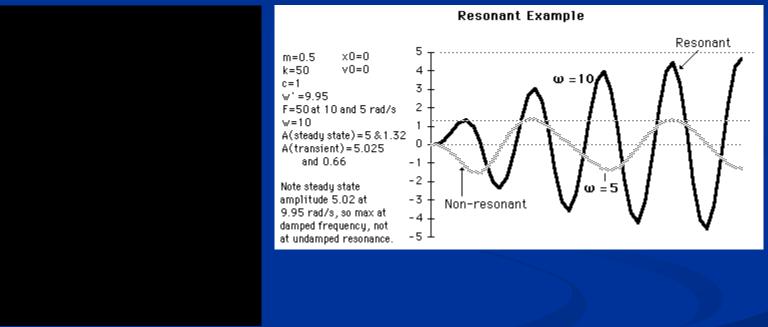
Things get exciting when the frequency of this oscillating pressure approach the natural frequency of the member

What is the 'natural frequency'?

"...a characteristic value of the driving frequency at which the amplitude of oscillation is a maximum."

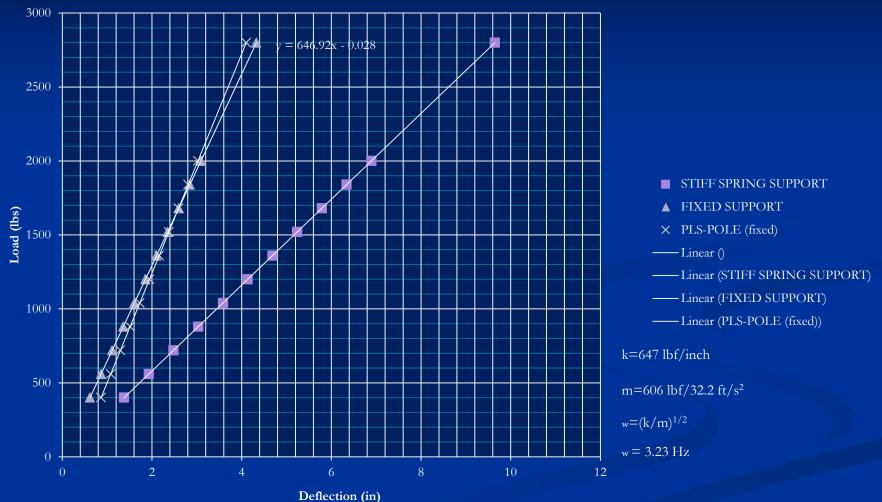


If a sinusoidal driving force is applied at the resonant frequency of the oscillator, then its motion will build up in amplitude to the point where it is limited only by the damping forces on the system. If the damping forces are small, a resonant system can build up to amplitudes large enough to be destructive to the system. Such was the famous case of the Tacoma Narrows Bridge, which was blown down by the wind when it responded to a component in the wind force which excited one of its resonant frequencies.





Hand Calculating Natural Frequency $w=(k/m)^{1/2}$





It is more accurate to build an F.E. model of the davit arm for a more accurate calculation of the natural frequency

> Small concentrated masses along the arm's length (hand-holds, vangs, etc) can be incorporated in the model



SHIELDWIRE ARM -- PAGE NO. 21

CALCULATED FREQUENCIES FOR LOAD CASE 1

MODE FREQUENCY(CYCLES/SEC) PERIOD(SEC) ACCURACY

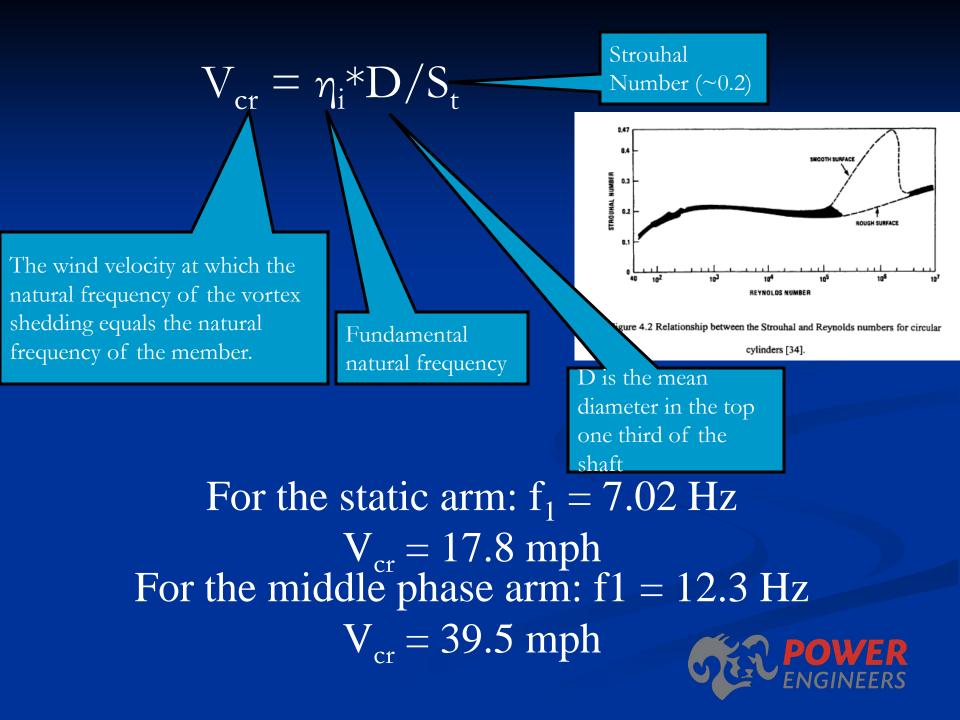
1	7.026	0.14234	2.217E-15
2	7.026	0.14234	8.168E-16
3	37.624	0.02658	2.152E-13
4	37.624	0.02658	5.859E-15
5	99.040	0.01010	6.275E-07



There are no standards in our industry that address any kind of wind-induced motion.

ASME Standard STS-1 (Steel Stacks) has a section on dynamic responses and sites Von Karman's relationship between critical wind velocities and the potential for vortex shedding:





It appeared that excitation wind speeds were very probable, especially on the static arms. We planned to proceed with analyzing the dynamic loads to determine the stresses at the weld connection. Concurrently, the independent metallurgical analysis issued the following statement that strengthened our perspective:

"...the root cause of the failures of the subject...shield wire arms was that the fatigue endurance limit of the columbium-vanadium steels, at the H.A.Z. (Heat Affected Zone) of the shaft material, was exceeded by the cyclic vibrational stresses to which the arms were subjected during the 39 days after installation."



A statement that begged further investigation instead brought closure and shut the investigation down.
The arms were replaced by the pole vendor, and 150 lb weights were added to the unloaded static arms.
We (temporarily) closed the books on this topic



Segue to 2011...





The 345 kV project in Wisconsin. Proposal to Utility: •Two pole suppliers are providing structures for the project.

•Two pole suppliers are providing structures for the project. POWER will build F.E. models of the shield wire arms and longer phase arms (middle phase) for both vendors that are supplying poles to the Project.

•Calculate the modal or natural frequencies associated with each unique arm – convert this to a modal excitation wind speed

•Approximate the lift and drag force along the arm due to this wind speed.

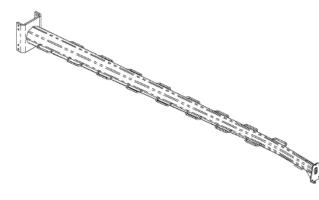
•Apply this lift force as a forcing function occurring at the resonant frequency

•Quantify the base reactions and convert those to a stress range. Compare that with recommended limits.

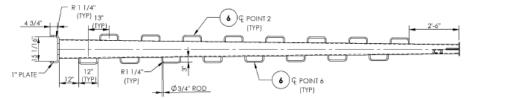
•Determine effective methods of damping the unloaded arms. GINEER

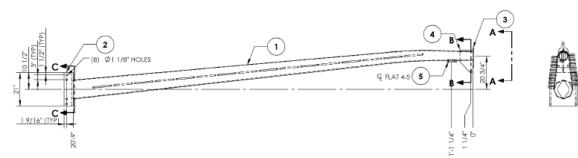
Part 1: Model Vendor 'A's tangent static arms

ARM INFORMATION												
ARM NO.	HOR. LENGTH	THICKNESS	LARGE DIA	SMALL DIA	RADIUS	ARC LENGTH	SMALL END STRAIGHT	RISE	SMALL END MITERED			
26482-AA	20'-9'	5/16"	12"	6"	20'-0"	27"	24"	20 3/4"	N			



PARTS AND ASSEMBLIES LIST										
ITEM NO.	PART NUMBER	QTY.	DESCRIPTION							
1	26482-7001	1	ARM SHANK							
2	26482-7101	1	ARM BRACKET							
3	26482-7201	1	ARM END PLATE							
4	26482-7301	1	THROUGH VANG							
5	26482-1501	1	S.S. GROUND PAD							
6	26482-7401	16	HAND GRAB							

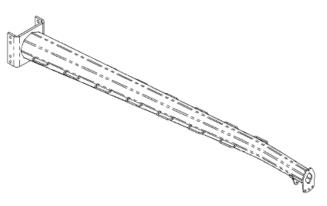




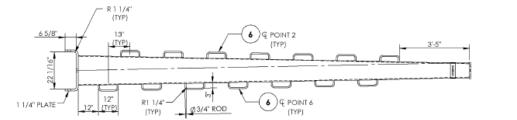
•20'-9" arm
•12" dia. base/6" dia. tip;
•5/16" thick octagonal plate
•Wt = 800 lbs

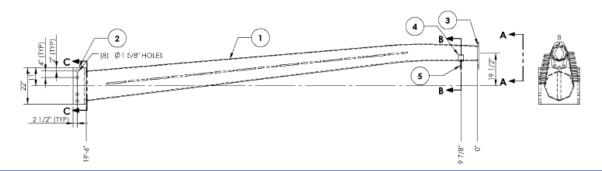
And middle phase arms:

ARM INFORMATION												
ARM NO.	HOR. LENGTH	THICKNESS	LARGE DIA	SMALL DIA	RADIUS	ARC LENGTH	SMALL END STRAIGHT	RISE	SMALL END MITERED			
26482-AC	19'-6"	3/8"	18"	9"	20'-0"	30"	24"	19 1/2"	N			



PARTS AND ASSEMBLIES LIST									
ITEM NO.	PART NUMBER	QTY.	DESCRIPTION						
1	26482-7003	1	ARM SHANK						
2	26482-7124	1	ARM BRACKET						
3	26482-7202	1	ARM END PLATE						
4	26482-7405	1	DOUBLER						
5	26482-7302	1	VANG						
6	26482-7401	14	HAND GRAB						

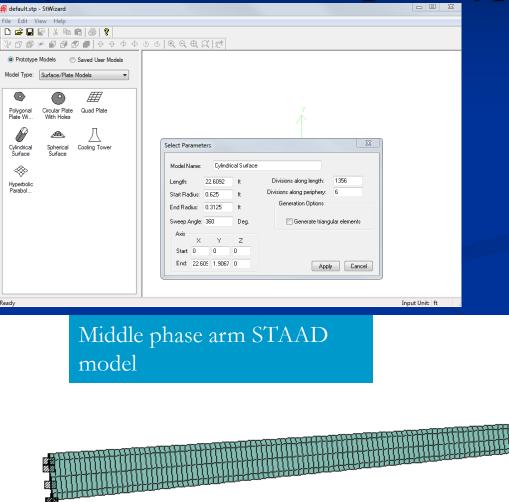




19'-6" arm
18" dia. base/9" dia. tip;
3/8" thick octagonal plate
Wt = 1,400 lbs

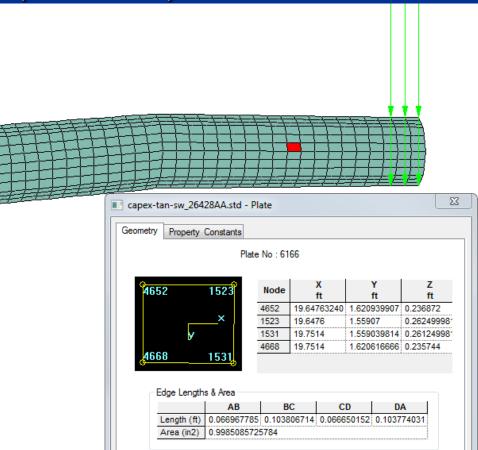


In order to calculate the modal frequencies, the arm is modeled in STAAD-Pro using cylindrical surface prototype models



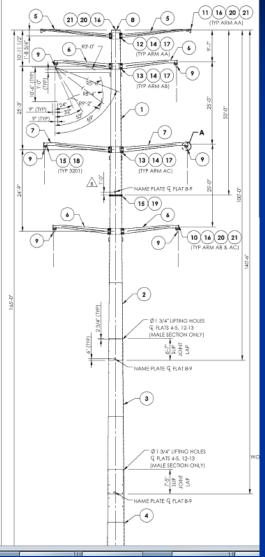


- Plate elements are sub-divided to create well-behaved elements (less than 4:1 length-width ratios)
- End plates and vangs are modeled as vertical loads. These loads must be applied in all three global directions when using a dynamic analysis to calculate the natural frequency





ARM NATURAL FREQUENCIES



Arm Type	1 st Natural Frequency, ŋ 1	2 nd Natural Frequency, ŋ 2	Excitation Wind Speed for 1 st mode	Excitation Wind Speed for 2 nd mode
Tangent Static Arm	6.97 Hz	33.23 Hz	17.8 mph	85 mph
Tangent Phase Arm (Middle)	12.3 Hz	61.9Hz	39.5 mph	184.0 mph

Steady state winds that will excite the middle phase arm (~40 mph) are much less likely to occur than those speeds that will induce motion in the static arms (~18 mph). For simplicity and WOLOG, we will focus on the static wire arms.



Aerodynamic Forces on an

arm

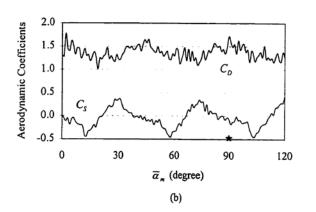


Figure 4.8 Aerodynamic coefficients for straight poles having a (a) hexagonal; and (b)

octagonal cross-section.

$$[M]{\{\ddot{Q}\}}_{j} + [C]{\{\dot{Q}\}}_{j} + [K]{\{Q\}}_{j} = {\{P\}}_{j}.$$

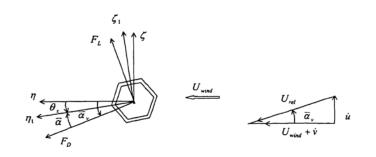


Figure 4.16 Aerodynamic forces per unit length of DE.

with

$$\overline{\alpha} = \overline{\alpha}_{y} - \theta_{x} \tag{4.24}$$

and

$$F_{D} = \frac{1}{2} \rho_{air} U_{rel}^{2} DC_{D}$$

$$F_{L} = \frac{1}{2} \rho_{air} U_{rel}^{2} DC_{S} .$$

$$(4.25)$$

 C_{ρ} and C_{s} are the same as before. The forces per unit length in the ζ_{1} and η_{1} directions are:

$$F_{\zeta_1} = -F_D \sin \overline{\alpha} + F_L \cos \overline{\alpha}$$

and

$$F_{n} = F_{D} \cos \overline{\alpha} + F_{L} \sin \overline{\alpha} . \qquad (4.26)$$

As before, the directions ζ and η are used for ζ_1 and η_1 , respectively.



A dynamic analysis in STAAD is capable of performing a modal response based on the second order differential equation for driven harmonic oscillators:

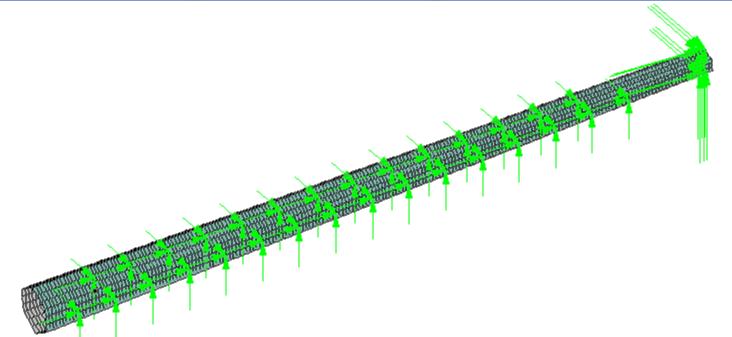
$$\ddot{x} + 2\beta\eta\dot{x} + \eta^2x = F(t)/m$$

In this equation, β is the damping ratio and **h** is the natural frequency. The damping is the sum of the inherent structural damping (β s) and the aerodynamic damping (β a). The aerodynamic damping can be a negative value by a phenomenon known as 'negative aerodynamic damping' wherein the motion-induced forces are in phase with the velocity component of the structure. If the sum (β s + β a) is less than zero, this increases amplitude and the associated stress ranges on the shaft.



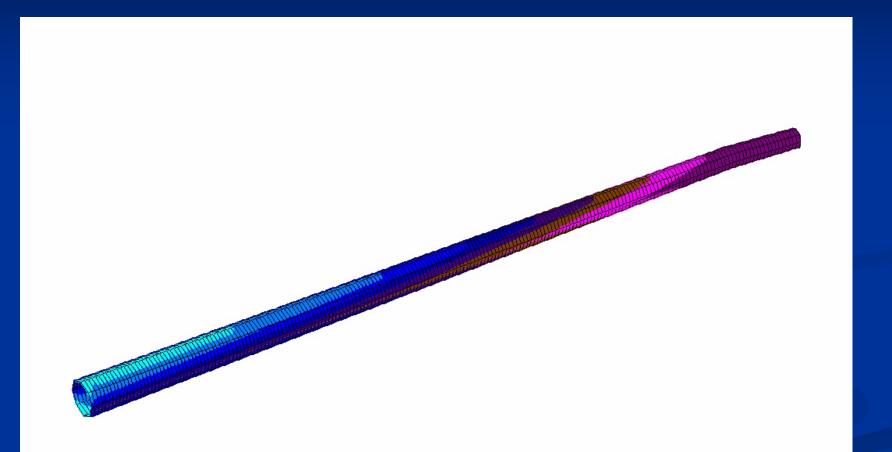
where F (z,t) = $1/2C_{L}*\varrho^{*}u(z)^{2*}D(z)*\cos(\eta_{i}t + \zeta(t))$

This is calculated and applied as discrete loads at nodes along the arm's length.



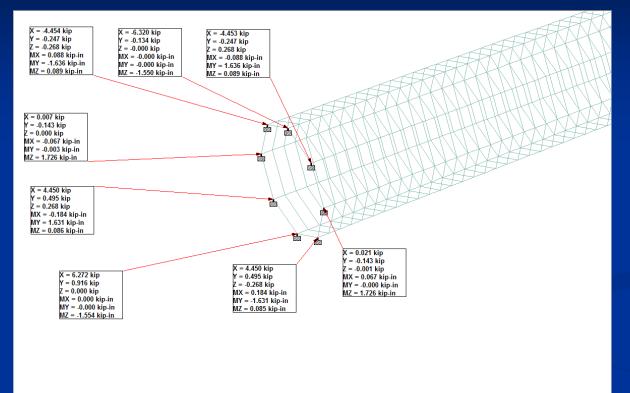


Arm motion and stress contours:





Finite Element Model reactions



•M=Sfxi*zi •Fb = M/S

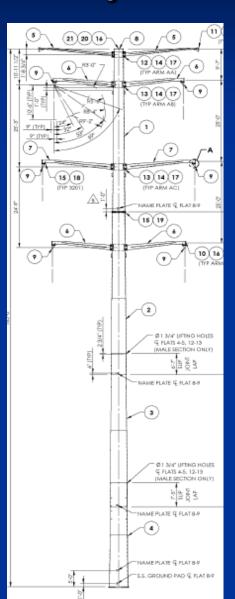
Load 3

Ĭ_źx

Forcing function is applied as a time history load in the (+) and (-) y direction and combined with the gravity loads. The cyclic stress range is determined by taking the difference in the two resulting reactions.

POWER ENGINEERS

Dynamic Stress Approximation:



Vendor A	Length	Weight	Base/Tip O.D.	Dynamic Stress Range- undamped	Dynamic Stress Range- 50 lb damper	Dynamic Stress Range- 100 lb damper
Tangent Static Arm	20′-9″	800 lbs	12"/6"	12.4 ksi	2.9 ksi	1.6 ksi

Arm Specifications and Calculated Stresses



FIELD TESTING:

•ESI Engineering, INC performed an experimental modal analysis with the following goals:
•Determine the natural frequencies of the static and middle-phase arm
•Determine the (structural) damping in each arm

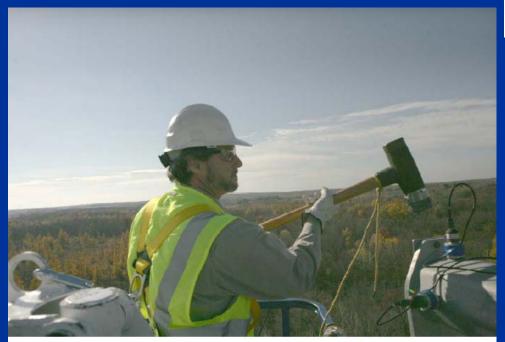


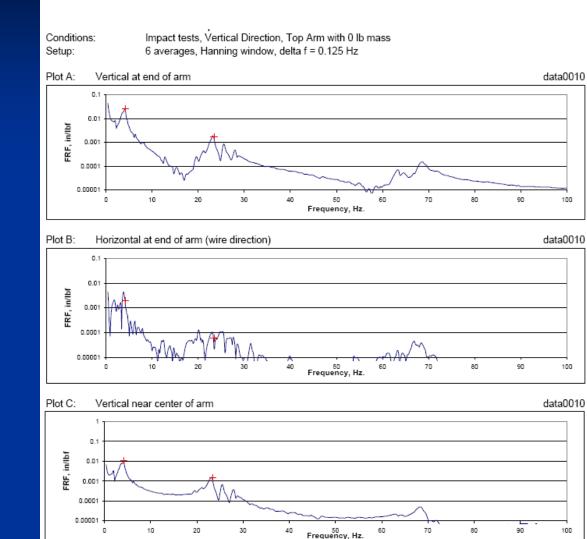
Figure 3 – Photograph showing a vertical impact of a davit arm with the modal impact hammer.



Figure 1 – Photograph of transmission pole 125 tested.

This field measurement consisted of a modal impact hammer, three accelerometers, and a FFT (Fast Fourier Transform) to get the FRF (Frequency Response Function)





Field data for static arm after the FFT. The red crosshairs indicate the modal frequencies



The field set-up and results:

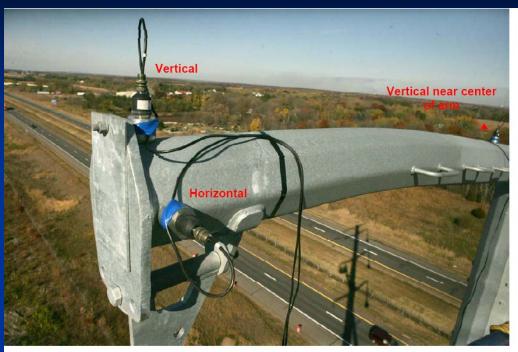


Figure 2 – Photograph of the middle conductor davit arm showing the accelerometer orientation.

Table 1 – Summary of Vertical Direction Measurement Results and Figure Numbers

Top Shield	Appendix A	Mo	ode 1	Mo	ode 2
Davit Arm	Figure No.	Frequency, Hz	% Critical Damping	Frequency, Hz	% Critical Damping
0 lb	Fig. 15 & 16	4.125	4.8	23.250	1.4
50 lbs	Fig. 11 & 12	3.625	6.8	21.125	1.9
100 lbs	Fig. 9 & 10	3.500	6.5	19.625	1.1
	-				
Middle Conductor	Appendix A	Mo	ode 1	Mo	ode 2
Davit Arm	Figure No.	Frequency, Hz	% Critical Damping	Frequency, Hz	% Critical Damping
0 lb	Fig. 5 & 6	5.500	3.7	38.000	1.2
50 lbs	Fig. 3 & 4	5.125	3.3	35.375	0.7
100 lbs	Fig. 1 & 2	4.625	10.9	33.000	1.5

Adjustments to the STAAD models

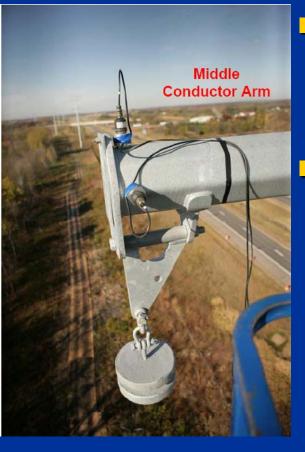
 Acknowledging that the base of the arm is not truly 'fixed', we adjusted the supports to have a spring constant of 2400 kip/ft in all three axes to match the field measured natural frequencies of the bare arm. The modal frequencies with 50lb and 100lb weights were checked against field measured values with good agreement.

Tangent	Tangent	Tangent Static Arm
•	Static Arm	STAAD
Static Arm		
Measured	Calculated	w/spring
		supports
4.125 Hz	3.23 Hz	4.133 Hz



Damping

Damping was a larger concern. The experimental procedure induced erroneous readings. Damping values affect cyclic stress values at the base of the arm.

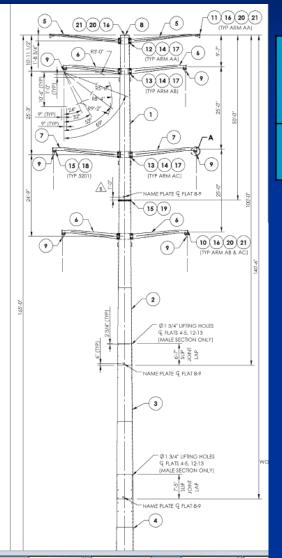


Initially assumed a value of .03, modified this to .019 based on field results and client input

Slack rope effect' with suspended weights made the measured values suspect:

Top Shield	Appendix A	M	ode 1
Davit Arm	Figure No.	Frequency, Hz	% Critical Damping
0 lb	Fig. 15 & 16	4.125	4.8
50 lbs	Fig. 11 & 12	3.625	6.8
100 lbs	Fig. 9 & 10	3.500	6.5
	-		
Middle Conductor	Appendix A	Me	ode 1
Davit Arm	Figure No.	Frequency, Hz	% Critical Damping
0 lb	Fig. 5 & 6	5.500	3.7
50 lbs	Fig. 3 & 4	5.125	3.3
100 lbs	Fig. 1 & 2	4.625	10.9

MODIFIED RESULTS



Original results:

Arm Type	Length	Weight	Base/Tip O.D.	Dynamic Stress Range- undamped	Dynamic Stress Range- 50 Ib damper	Dynamic Stress Range-100 Ib damper
Tangent Static Arm	20'-9"	800 Ibs	12"/6"	12.4 ksi	2.9 ksi	1.6 ksi

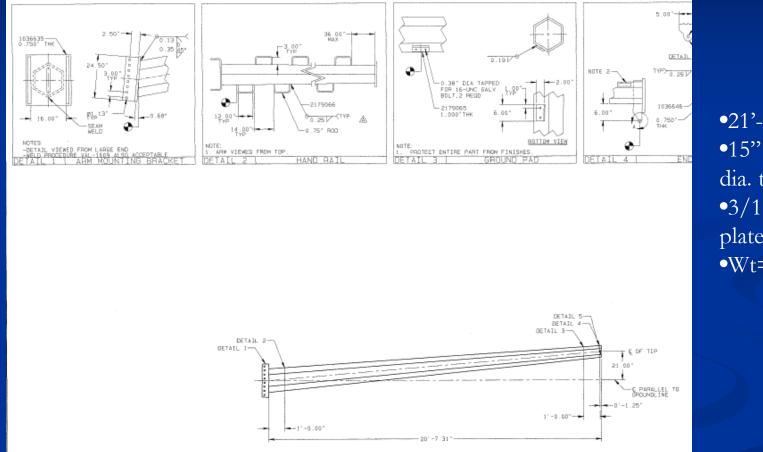
Stresses with adjusted modal frequency and damping:

Arm Type	Length	Weight	Base/Tip O.D.	Dynamic Stress Range- undamped	Dynamic Stress Range- 50 Ib damper	Dynamic Stress Range-100 Ib damper
Tangent Static Arm	20'-9"	800 Ibs	12"/6"	8.0 ksi	1.6 ksi	0.8 ksi



Part 2: Model Vendor B's static

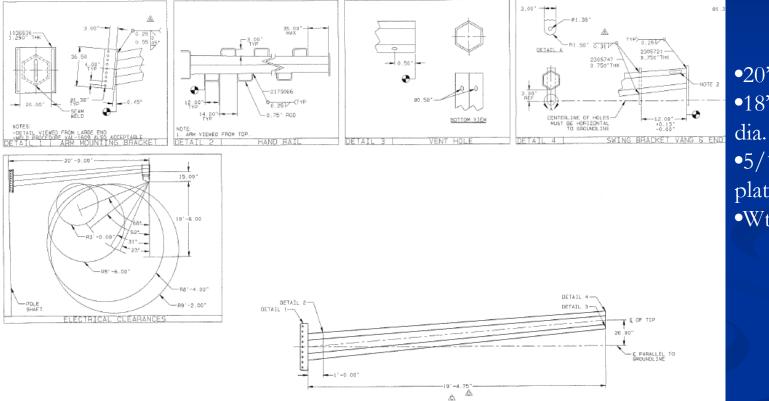
arm:



•21'-0" arm
•15" dia. base/ 7.5" dia. tip
•3/16" hexagonal plate
•Wt=756 lbs



And phase arm:



•20'-0" arm •18" dia. base/ 12" dia. tip •5/16" hexagonal plate •Wt=1,627 lbs



ARM NATURAL FREQUENCIES

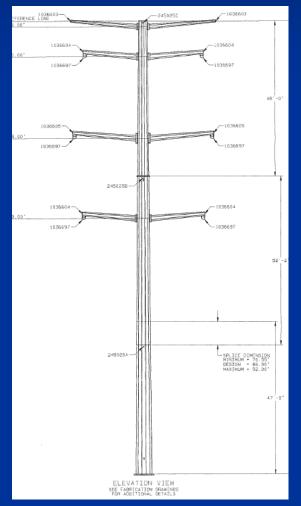
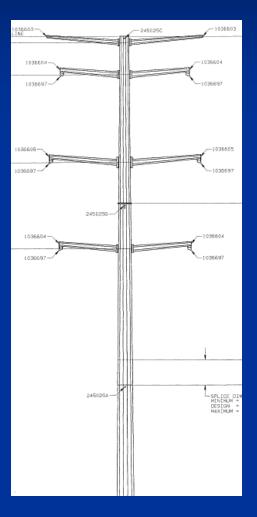


Table 1: Arm Modal Frequencies						
Arm Type	1 st Natural Frequen cy , ŋ 1	2 nd Natural Frequen cy, ŋ 2	Excitation Wind Speed for 1 st mode	Excitation Wind Speed for 2 nd mode		
Tangent Static Arm	9.6 Hz	45.4 Hz	31.0 mph	145.1 mph		
Tangent Phase Arm (Middle)	12.04 Hz	49.24 Hz	38.4 mph	156.6 mph		

Hexagonal arms have a higher first mode natural frequency. Thus a greater steadystate wind speed is required to induce motion.



Dynamic Stress Approximation:



Arm Type	Length	Weight	Base/Tip O.D.	Dynamic Stress Range- undamped	Dynamic Stress- 50 Ib damper	Dynamic Stress-100 Ib damper
Tangent Static Arm	20′-7″	756 lbs	15″/7.5″	39 ksi	7.8 ksi	4.2 ksi

Arm Specifications and Calculated Stresses



Continued Field Testing:

•Test the shield wire arms from the Vendor B

•Improved the mass attachment to avoid 'slack rope' nonlinearity during the measurements.

•Investigated the effectiveness of tying the arms together during this exercise.





Results:

Top Shield	Appendix A	Mode 1			
Davit Arm	Figure No.	Frequency, Hz	% Critical Damping		
0 lb	Fig. 1 & 2	6.375	2.3		
50 lbs	Fig. 3 & 4	6.000	1.8		
100 lbs	Fig. 5 & 6	5.000	2.0		
Cable - 7.00" Gap	Fig. 25 & 26	8.250	2.4		
Cable - 6.75" Gap	Fig. 27 & 28	8.250	1.4		
Cable - 6.00" Gap	Fig. 29 & 30	8.250	1.3		
Middle Conductor	Appendix A	Mode 1			
Davit Arm	Figure No.	Frequency, Hz	% Critical Damping		
0 lb	Fig. 7 & 8	8.750	1.3		
50 lbs	Fig. 9 & 10	8.375	1.6		
100 lbs	Fig. 11 & 12	8.125	2.2		
Cable - 6.00" Gap	Fig. 31 & 32	8.250	1.8		

•These hexagonal arms have a higher 1st modal frequency which implies a higher steady-state wind speed is required to induce motion from vortex shedding.

•Different spring constants at the support were required to match the field measured modal frequencies. This is due to the difference in the arm connection.

•Note that changing the tensions in hold-down cables does not affect the modal frequency. The upper/lower arm system adopts a frequency close **OWER** to that of the lower arm.

Dynamic stress comparison's with spring supports and adjusted % critical damping

Arm Type	Length	Weight	Base/Tip O.D.	Dynamic Stress Range- undamped	Dynamic Stress Range- 50 Ib damper	Dynamic Stress-100 lb damper
Vendor A	20'-9"	800 lbs	12"/6"	8.0 ksi	1.6 ksi	0.8 ksi
Vendor B	20'-9"	756 lbs	15"/7.5"	34.7 ksi	9.6 ksi	4.1 ksi

•The fixity and critical damping were altered based on field measurements for Vendor B's arms.

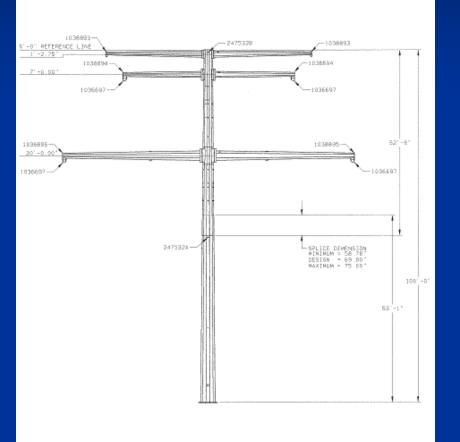
•The above table compares stress ranges. NOTE: This does not imply that Vendor A's arms are superior! Recall the required steady-state wind speeds:

•Vendor A: 9 mph

•Vendor B: 21 mph



Part 3: Analyze a Modified Configuration



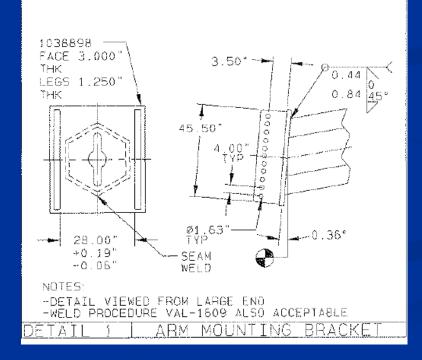
Static Arm: •28'-0" arm •18" dia. base/ 9" dia. tip •7/32" hexagonal plate •Wt=1,259 lbs

Lower phase arm: •40'-0" arm •28" dia. base/ 15" dia. tip •1/2" hexagonal plate •Wt=6,729 lbs



Lower phase arm is a different animal than anything studied to-date:

- 3" 'base plate'
- •Mounted at a lower elevation
- (stiffer section of pole)Can we assume the same spring constants at the supports that were used for previous models?





Static and lower phase arm results:

Arm Type	1 st Natural Frequency, η 1	2 nd Natural Frequency, η ₂	Excitation Wind Speed for 1 st mode	Excitation Wind Speed for 2 nd mode
Tangent Shield Wire Arm	4.3 Hz	22 Hz	16.5 mph	86.1 mph
Tangent Lower Phase Arm	2.7 Hz	17 Hz	16.3 mph	103.8 mph

Static arm follows same trend as previously tested static arms
Note that the massive phase arm has a low first mode excitation wind speed.
These arms will be field tested soon (today, in fact).





POW

Lower Phase
Arm39'-4"6,729
lbs28"/15
"24.1 ksi17.6 ksi13.5 ksi12.1 ksi

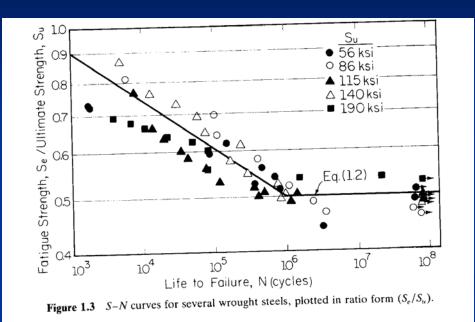
But what do these stress ranges mean...

The Fundamentals of Metal Fatigue Analysis

Definition: Metal fatigue is a process which causes premature failure or damage of a component subjected to repeated loading.



Typical S-N curve for wrought Steels



For A572 Gr 65 Steel, Su = 80ksi

Other factors affecting the shape of an S-N curve:

- •Loading Effects (variable amplitude load)
- •Surface finish
- •Size (Thickness adversely affects fatigue strength in welds)
- •Se' (modified endurance limit) = $S_e * C_{size} * C_{load} * C_{surf. finish...}$



AVAILABLE CODES ADDRESSING FATIGUE:

1. AASHTO FATIGUE CURVES

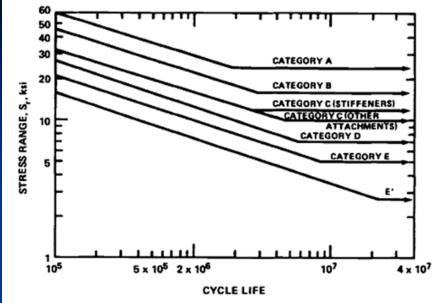


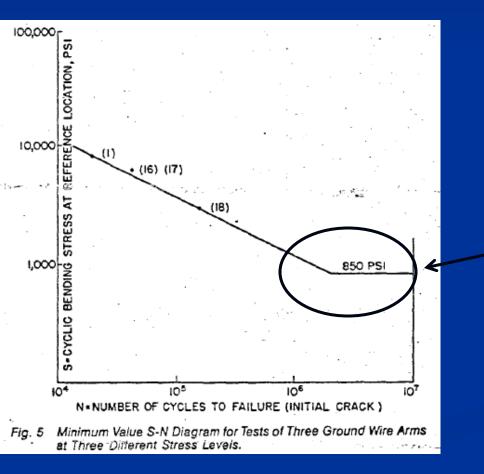
FIG. 10.23 Design stress range curves for categories A to E'.

Various curves depend on weld geometry and plate thickness. E' is for thick plate

2. AISC Appendix K: •Load Condition 4: $2x10^6$ cycles •Stress Category C • $F_{th} = 10$ ksi (the magnitue of the change in stress due to the application or removal of the unfactored live load). 3. IEC • $F_{th} = 5$ ksi



S-N curve based on laboratory testing shield wire arms at three different stress levels to initial crack



In 1979, IEEE released a report on the effects of dynamic loading on arms. Three static arms were tested in the laboratory at different stress levels to produce the S-N curve on the left.

If arms are to be vacant for a few years, we would want to be in this area of the graph.



CONCLUSIONS:

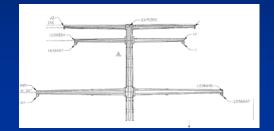
•The F.E. analysis in conjunction with parameters from field measurements shows that tuned-mass damping is effective in reducing stress levels, but many utilities are looking at other options. The weights themselves cost \$3/lb. On a large scale project, this can quickly become a substantial cost.

•Explore the use of mass-particle damping. For instance, sand or a chain inside the arm. Energy is dissipated through the friction associated with particle interaction.

•Further explore the costs and pros/cons of tying arms together

•These F.E. models are discrete approximations at this point.

•The models require further refinement with the assistance of additional field testing and preferably low-speed wind tunnel testing. The field testing does not incorporate the aerodynamic damping, βa , which can be negative.



Mass Particle damping may work better than tuned mass damping for a 40' arm weighing 6,700 lbs.



Factor in Dynamic Loading Criteria

•The IEEE paper found that the best ways to minimize fatigue failure are as follows:

1. Eliminate the drain hole that acts as a stress concentration factor

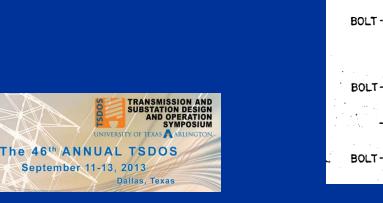
SIDE VIEW

(TOP VIEW)

ORIGINAL DESIGN MODIFIED DESIGN

- 2. Do not allow arms to be galvanized due to residual stresses
- 3. Use thicker arm connection plates

BOLT



The method that suppliers use to design and fabricate arms has not changed in over 40 years and therefore is unlikely to change. When a project involves unloaded arms or arms that may vibrate due to galloping conductors, we, as engineers, would be well advised to consider specifications that include dynamic loading criteria and preventative measures that can be built into the design and fabrication process.

•Collect wind data as close to the project site as possible. Use it to determine if there is a potential issue. Remember that arm vibrations can also be caused by galloping conductors. The magnitude of the driving force is not necessarily large.

Do not force vendors (via conductor configurations or pole geometry) to design an arm that may have a short service life due to dynamic loading.
Determine the steady-state wind speed that will induce vortex shedding. Typically, most phase arms are short and heavy with 1st mode frequencies that correlate to rare steady-state wind conditions.





THANK YOU!

QUESTIONS?



The 46th ANNUAL TSDOS September 11-13, 2013 Dallas, Texas